

Feb. 12, 1952

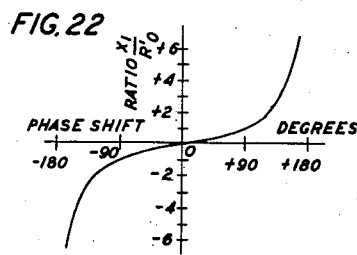
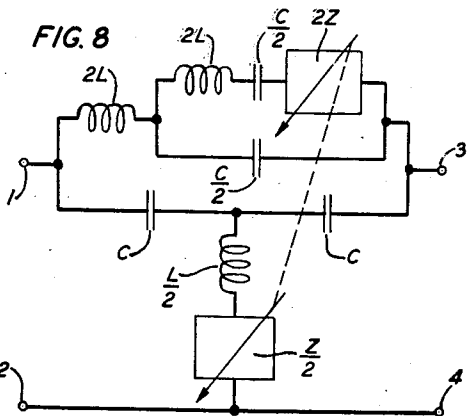
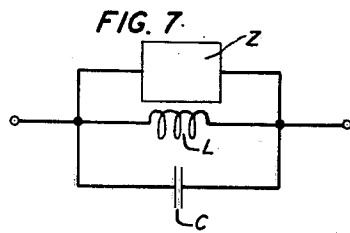
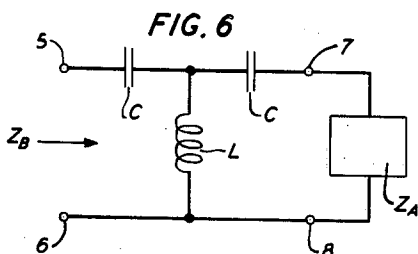
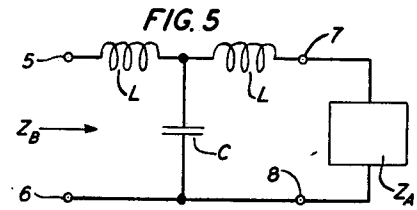
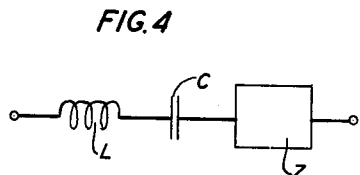
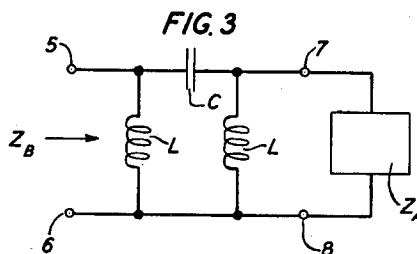
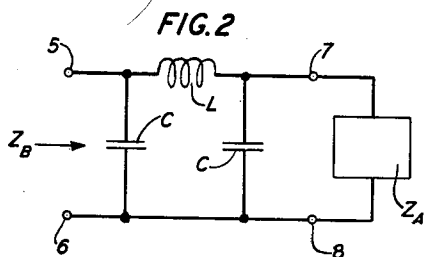
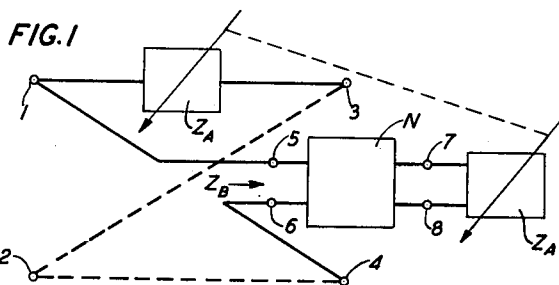
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2,585,842

BRIDGED T PHASE SHIFTER

Original Filed Sept. 22, 1949

3 Sheets-Sheet 1



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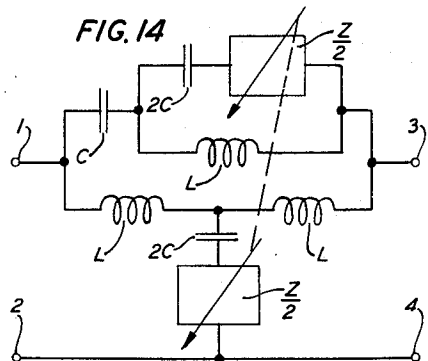
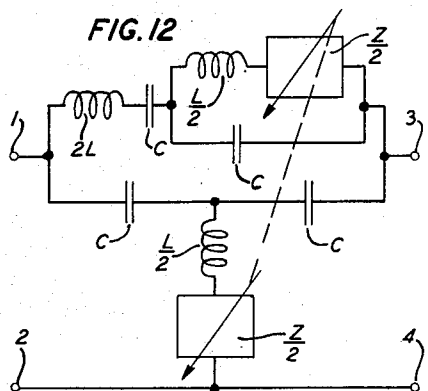
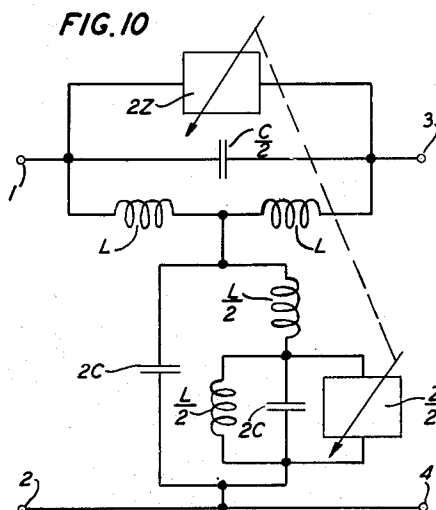
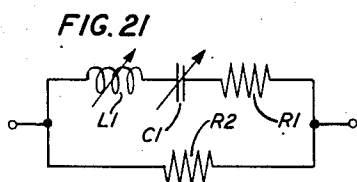
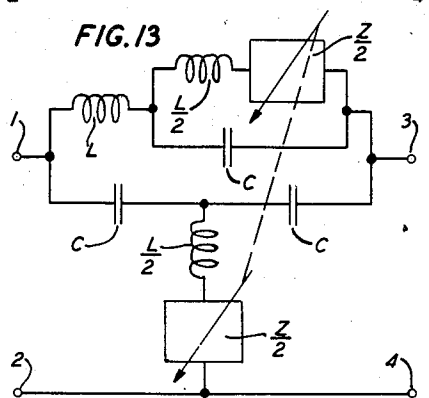
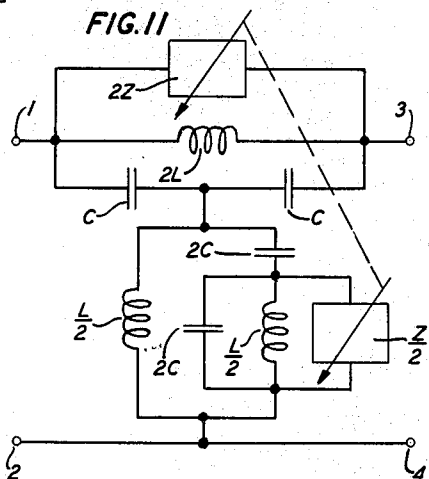
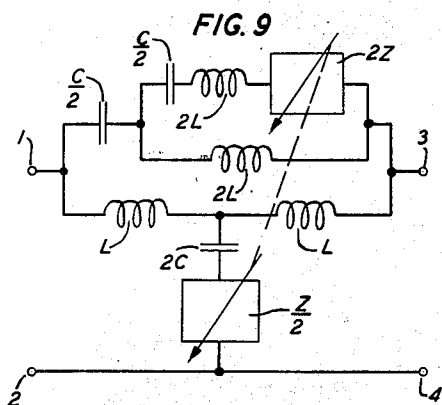
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2,585,842

BRIDGED T PHASE SHIFTER

Original Filed Sept. 22, 1949

3 Sheets-Sheet 2



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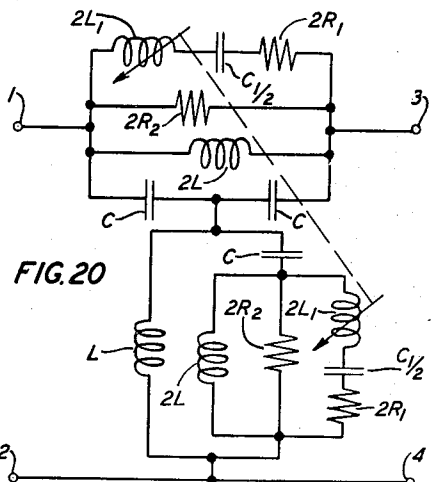
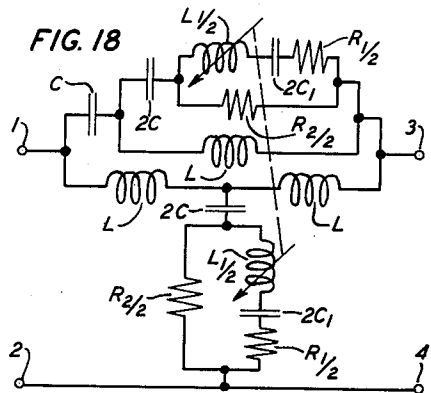
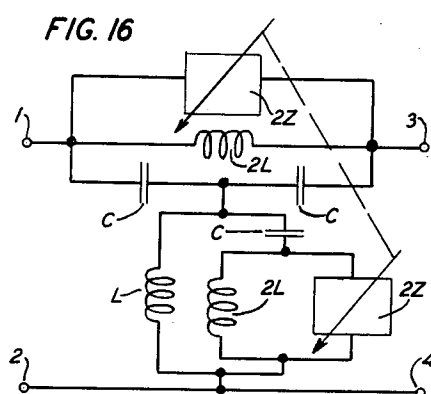
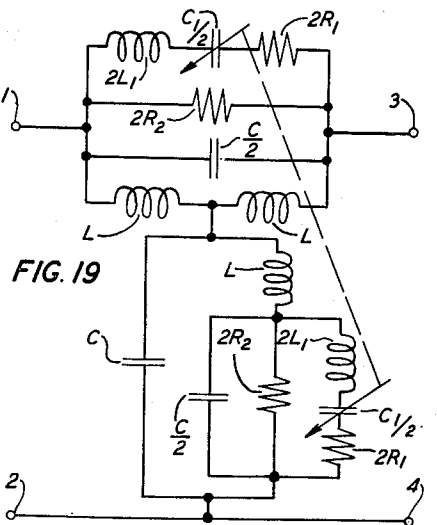
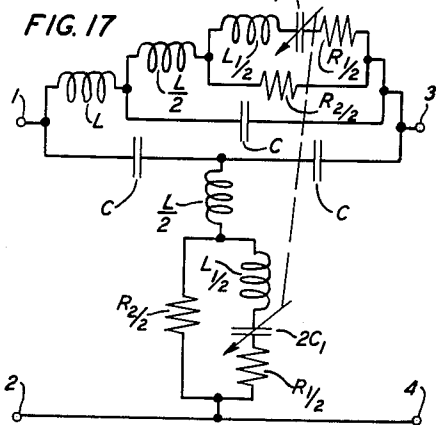
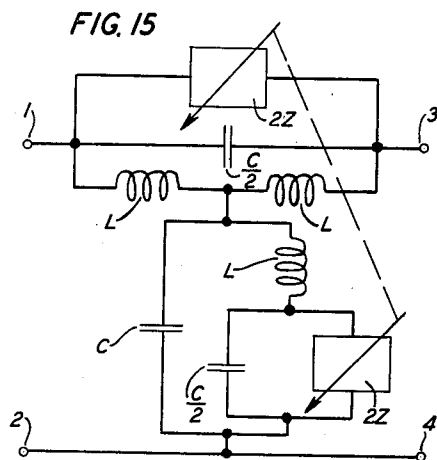
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2,585,842

BRIDGED T PHASE SHIFTER

Original Filed Sept. 22, 1949

3 Sheets-Sheet 3



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2,585,842

BRIDGED T PHASE SHIFTER

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Original application September 22, 1949, Serial
No. 117,255. Divided and this application Sep-
tember 29, 1950, Serial No. 187,493

23 Claims. (Cl. 178-44)

1

This invention relates to wave transmission networks and more particularly to variable phase shifters.

An object of the invention is to vary the phase shift of a wave transmission network over a wide range without changing its image impedance.

Another object is to maintain a constant insertion loss at all settings of such a phase shifter.

Other objects are to simplify the circuit and reduce the size and cost of phase shifters of this type.

This is a division of my copending application Serial No. 117,255, filed September 22, 1949.

There is often required a wave transmission network in which the phase shift at a single frequency may be varied without changing the insertion loss or the image impedance. Such a device may be built in the form of a constant-resistance structure but, in order to keep the image impedance constant, both variable inductors and variable capacitors are required.

The variable phase shifter of the present invention has the advantage that only a single type of variable reactor, either a capacitor or an inductor, is required. In the unbalanced form only two variable reactors are required and their reactances are equal at each setting. The circuit is of the bridged-T type. It is derived from a constant-resistance, all-pass, lattice network in which one branch comprises a general reactive impedance and the other branch comprises an equal impedance connected to the remote end of a subsidiary network which has a phase shift of 90 degrees or an odd multiple thereof at the operating frequency f_0 and thus effects an inversion of the impedance. The subsidiary network may, for example, be a T or π of reactances forming a low-pass or a high-pass filter. In order to provide a wide range of phase shift, in one embodiment the general impedance includes both a capacitor and an inductor, connected either in series or in parallel, one of which is variable. To facilitate the transformation from lattice to bridged-T, one or more additional reactors may be added arbitrarily to the general impedance. By a special procedure the lattice may be transformed into an equivalent bridged-T network in which exactly equal variable reactances appear in both the bridging branch and the shunt branch. Since these variable reactances remain equal at all settings of the phase shifter they may conveniently be arranged for unitary control. In order to maintain the insertion loss substantially constant at all settings, compensating resistors may be added to the bridging and shunt branches.

2

The nature of the invention will be more fully understood from the following detailed description and by reference to the accompanying drawing, in which like reference characters are used to designate similar or corresponding parts and of which:

Fig. 1 is a schematic circuit of the prototype constant-resistance lattice network in which the series branch is a general impedance Z_A and the diagonal branch Z_B comprises a second impedance Z_A associated with a subsidiary impedance inverting network N;

Figs. 2 and 3 show the branch Z_B when the network N is a π -type low-pass or high-pass filter, respectively;

Fig. 4 shows a series type of general impedance Z_A suitable for use with the π -type networks N of Figs. 2 and 3;

Figs. 5 and 6 show diagonal branches Z_B comprising T-type filters;

Fig. 7 shows a parallel type of general impedance Z_A suitable for use with the T-type networks N of Figs. 5 and 6;

Fig. 8 is a schematic circuit of a bridged-T network equivalent, except for an interchange of branches, to the prototype lattice of Fig. 1 when the subsidiary network N is a π -type low-pass filter as shown in Fig. 2 and the general impedance Z_A is the series type shown in Fig. 4;

Fig. 9 is a network similar to the one shown in Fig. 8 except that the high-pass filter of Fig. 3 is substituted for the low-pass filter;

Fig. 10 is a bridged-T network equivalent to the lattice of Fig. 1 when N is a T-type low-pass filter as shown in Fig. 5 and Z_A is the parallel type of Fig. 7;

Fig. 11 is a network similar to the one shown in Fig. 10 except that the high-pass filter of Fig. 6 is substituted for the low-pass filter;

Fig. 12 is a circuit equivalent to the one shown in Fig. 8 after a portion of the bridging branch has undergone an impedance transformation to provide equal variable impedance $Z/2$ in the bridging and shunt branches;

Fig. 13 is a preferred embodiment of the invention, equivalent at the operating frequency f_0 to the circuit of Fig. 12, in which one of the capacitors C in the bridging branch has been eliminated;

Figs. 14, 15, and 16 are other preferred embodiments derived, respectively, from the circuits shown in Figs. 9, 10, and 11;

Figs. 17, 18, 19, and 20 are specific circuits corresponding, respectively, to those shown in Figs. 13, 14, 15, and 16 when the variable imped-

ance Z is constituted by the series combination of the elements L_1 , C_1 , and R_1 in parallel with a compensating resistor R_2 , as shown in Fig. 21: and

Fig. 22 is a curve showing how the insertion phase shift of the network is related to the value of the variable reactance.

Taking up the figures in more detail, Fig. 1 shows schematically the prototype lattice network comprising two equal generalized series impedance branches Z_A and a pair of equal diagonal impedances Z_B connected between a pair of input terminals 1, 2 and a pair of output terminals 3, 4. Only one series branch Z_A and one diagonal impedance Z_B are shown explicitly, the other corresponding branches being indicated by the broken lines connecting the appropriate terminals. A suitable source of alternating electromotive force may be connected to the input terminals and a load or utilization circuit connected to the output terminals.

The impedance Z_B is made up of a reactive four-terminal subsidiary network N connected to the diagonal branch at the terminals 5, 6 and terminated at its output terminals 7, 8 in an impedance Z_A of the same value as the impedance forming the series branch of the lattice. The function of the subsidiary network N is to invert the impedance Z_A with respect to R_o , the image impedance of the lattice, and therefore N also has an image impedance equal to R_o and an image phase constant which is equal to an odd multiple of 90 degrees.

If the impedance Z_A is essentially a pure reactance of value X_A the lattice network will operate as a phase shifter having an image impedance R_o and an insertion phase shift β given by

$$\beta = 2 \tan^{-1} \frac{X_A}{R_o} \quad (1)$$

It is seen, therefore, that the phase shift introduced depends upon the reactance of the impedances Z_A and may be varied by adjusting the value of X_A . As will be explained below, the effects of parasitic dissipation in the reactive elements forming Z_A can be compensated for to a large extent, so that the insertion loss of the lattice is substantially constant and independent of the value of X_A .

Fig. 2 shows the configuration of the branch Z_B when the network N is a π -type low-pass filter comprising a series inductance L with a shunt capacitance C connected at each end thereof. In order for the network N to have an insertion phase shift of 90 degrees at the operating frequency f_o the elements have the following values:

$$C = \frac{1}{2\pi f_o R_o} \text{ farads} \quad (2)$$

$$L = \frac{R_o}{2\pi f_o} \text{ henries} \quad (3)$$

Fig. 3 shows the branch Z_B when N is a π -type high-pass filter made up of a series capacitance C and two shunt inductances L , the values of which are given by Equations 2 and 3.

Fig. 4 shows a specific form of the impedance Z_A suitable for use with the π -type networks of Figs. 2 and 3 to permit the conversion of the prototype lattice of Fig. 1 to a physically realizable equivalent bridged-T network, as explained below. It comprises the series combination of an inductance L , a capacitance C and an impedance Z yet to be determined. The elements C and L have the values given by Equations 2 and 3.

At the operating frequency f_o , L and C are resonant so that the impedance of Z_A is equal to Z .

Fig. 5 shows the branch Z_B when N is a T-type low-pass filter made up of two series inductances L and an interposed shunt capacitance C , and Fig. 6 when N is a T-type high-pass filter constituted by two series capacitances C and an interposed shunt inductance L . Here, again, the values of C and L are found from Equations 2 and 3.

Fig. 7 shows a specific form for the impedance Z_A suitable for use with the T-type networks of Figs. 5 and 6 to permit the realization of a physical bridged-T network equivalent to the lattice of Fig. 1. It comprises the parallel combination of a capacitance C , an inductance L and an impedance Z . The elements C and L have the values given by Equations 2 and 3.

Fig. 8 shows a bridged-T network equivalent to a lattice in which each series branch has the configuration shown in Fig. 2, each diagonal branch is an impedance Z_A , and Z_A is of the form shown in Fig. 4. This lattice, it will be recognized, is the same as the one shown in Fig. 1 except that the branches Z_A and the branches Z_B are interchanged. The bridged-T network of Fig. 8 comprises two series capacitances C , an interposed shunt branch made up of an inductance $L/2$ and an impedance $Z/2$ in series, and a bridging branch composed of an inductance $2L$ in series with a capacitance $C/2$, the latter being shunted by the series combination of a second inductance $2L$, a second capacitance $C/2$ and an impedance $2Z$. The impedance from terminal 1 to terminal 3 of the bridged-T is exactly twice that of each series branch of the prototype lattice, and the impedance from terminals 1 and 3 taken together to terminals 2 and 4 is exactly half that of each diagonal branch of the lattice.

Fig. 9 shows another bridged-T network which is equivalent, at the frequency f_o , to the circuit of Fig. 8. It is derived from a prototype lattice in which the network N is a high-pass π -type filter, as shown in Fig. 3, and the impedance Z_A has the form shown in Fig. 4.

Fig. 10 shows an unbalanced bridged-T network which is the equivalent of the prototype lattice of Fig. 1 when the network N is a T-type low-pass filter, as shown in Fig. 5, and the impedance Z_A has the configuration shown in Fig. 7.

The bridged-T network of Fig. 11 is similar to the one shown in Fig. 10 except that it is derived from a prototype lattice in which the network N is a T-type high-pass filter as shown in Fig. 6.

Each of the circuits shown in Figs. 8, 9, 10 and 11 includes an impedance $2Z$ in the bridging branch and an impedance $Z/2$ in the shunt branch. In order to adjust the insertion phase of the network, these impedances are made variable, as indicated by the arrows, and for convenience may be coupled together under a single control, as indicated by the broken line connecting the arrows.

The construction and adjustment of the phase shifter can be further simplified by making the variable impedance in the bridging branch equal to the one in the shunt branch. Fig. 12 shows how the circuit of Fig. 8 may be modified to accomplish this by introducing an impedance transformation into the bridging branch. This involves taking the capacitance $C/2$ out of the upper parallel arm, doubling its value, and placing it on the outside next to the capacitance $2L$. The

5

inductance $2L$ in the upper arm now becomes $L/2$ and the impedance $2Z$ becomes $Z/2$. In the lower arm, the capacitance $C/2$ becomes C . In Fig. 12 the two variable impedances $Z/2$ are now equal at all settings. The circuit of Fig. 12 is the exact equivalent of the one shown in Fig. 8.

Fig. 13 shows a further simplification that can be made in the circuit of Fig. 12 by removing the capacitance C next to the inductance $2L$ and reducing the value of the latter to L . At the operating frequency f_0 an inductance L has the same impedance as the series combination of an inductance $2L$ and a capacitance C . That this is true is apparent from the following considerations. First, divide the inductance $2L$ into two equal parts, L and L . Now one inductance L will resonate with C at f_0 and the combination will have zero reactance. Therefore, C and one of the inductances L may be removed, leaving only the other inductance L , as shown in Fig. 13 which is a preferred embodiment of the invention.

Fig. 14 shows another preferred embodiment obtained from the circuit of Fig. 9 in the same way that Fig. 13 is obtained from Fig. 8.

Figs. 15 and 16 are two other preferred embodiments of the invention obtainable by appropriate transformations of the networks of Figs. 10 and 11, respectively, in a manner analogous to that described above in connection with Figs. 12 and 13. In the circuits of Figs. 15 and 16 the variable impedances in the bridging and shunt branches are equal but each is equal to $2Z$ instead of $Z/2$ as in the networks of Figs. 13 and 14. The networks of Figs. 15 and 16 are electrically equivalent to the prototype shown in Fig. 1.

All that remains to be determined is the configuration of the general impedance Z . This may include only a single variable reactance, either an inductance or a capacitance. However, Z preferably comprises an inductance L_1 and a capacitance C_1 connected in series, as shown in Fig. 21. These preferably resonate at f_0 and either or both may be variable. The series resistance R_1 represents the effective resistance of the elements L_1 and C_1 at f_0 for an average setting of the adjustable element or elements. The shunting resistance R_2 is included to compensate the effect of the resistance R_1 and its value is so chosen, as explained below, that the insertion loss of the phase shifter is substantially independent of the setting of the adjustable element.

Figs. 17, 18, 19 and 20 show complete phase shifting networks in accordance with the invention corresponding, respectively, to the circuits of Figs. 13, 14, 15 and 16 when the impedance Z has the configuration shown in Fig. 21. In Fig. 17 the variable element in the bridging branch and the variable element in the shunt branch, under unitary control, are the capacitances $2C_1$. In Fig. 18 these elements are the inductances $L_1/2$, in Fig. 19 they are the capacitances $C_1/2$, and in Fig. 20 they are the inductances $2L_1$.

The performance of the phase shifters shown in Figs. 17, 18, 19 and 20, at the operating frequency f_0 , is best described in terms of the prototype lattice of Fig. 1. As already stated, Figs. 19 and 20 are the equivalent of Fig. 1, and Figs. 17 and 18 are equivalent to Fig. 1 if the series and diagonal branches of the lattice are interchanged.

In Fig. 1 it will be assumed that the network N has a phase shift of 90 degrees, or an odd multiple thereof, at f_0 , that the impedance Z_A has

6

the configuration shown in Fig. 4 or Fig. 7, and that the impedance Z has the form shown in Fig. 21. Since L and C are resonant in Fig. 4 and antiresonant in Fig. 7, the impedance Z_A will be equal to the impedance Z at f_0 . Therefore, in Fig. 1, the insertion loss α in nepers and the insertion phase shift β in radians are given by the expression

$$\epsilon^{\alpha+i\beta} = \frac{R_o + Z}{R_o - Z} \quad (4)$$

which may also be written in terms of the admittance Y as

$$\epsilon^{\alpha+i\beta} = \frac{R_o Y + 1}{R_o Y - 1} \quad (5)$$

where

$$Y = \frac{1}{Z}$$

In the case under consideration

$$Y = \frac{1}{R_2} + \frac{1}{R_1 + jX_1} \quad (7)$$

and

$$X_1 = 2\pi f_0 L_1 - \frac{1}{2\pi f_0 C_1} \quad (8)$$

so we have the relation

$$\epsilon^{\alpha+i\beta} = \frac{\frac{R_o}{R_2} + \frac{R_o}{R_1 + jX_1} + 1}{\frac{R_o}{R_2} + \frac{R_o}{R_1 + jX_1} - 1} \quad (9)$$

Now, if we set

$$\frac{1}{R_1} + \frac{1}{R_2} = \frac{R_2}{R_o^2} \quad (10)$$

Equation 9 may be written as

$$\epsilon^{\alpha+i\beta} = \frac{\left(\frac{R_2}{R_o} + 1\right)\left(\frac{1}{R_o} + j\frac{X_1}{R_1 R_2}\right)}{\left(\frac{R_2}{R_o} - 1\right)\left(\frac{1}{R_o} - j\frac{X_1}{R_1 R_2}\right)} \quad (11)$$

from which

$$\epsilon^{\alpha} = \frac{\frac{R_2}{R_o} + 1}{\frac{R_2}{R_o} - 1} \quad (12)$$

and

$$\beta = 2 \tan^{-1} \frac{X_1 R_o}{R_1 R_2} \quad (13)$$

It is seen from Equation 12 that the insertion loss is independent of the value of X_1 when R_1 and R_2 satisfy the relationship (10). Therefore, if the effective resistance R_1 associated with the elements C_1 and L_1 does not change with X_1 and if the compensating resistance R_2 is determined by Equation 10 the loss does not change as the phase shift β is varied. In practice it is found that R_1 does not change appreciably as X_1 is varied, especially if X_1 is varied by adjusting the capacitance C_1 , as in Figs. 17 and 19. To minimize the change in R_1 these capacitances are preferably furnished by capacitors having air as the dielectric.

From Equations 13 and 10 the following expression may be derived:

$$\beta = 2 \tan^{-1} \frac{X_1}{R_o'} \quad (14)$$

where

$$R_o' = \frac{R_o}{2} \left(1 + \sqrt{1 + \frac{4R_1^2}{R_o^2}} \right) \quad (15)$$

It is clear, therefore, that the phase shift β can be determined when the reactance X_1 , the resistance R_1 and the image impedance R_0 are known. The curve of Fig. 22 shows the phase shift β in degrees plotted against the ratio X_1/R_0 . If the reference phase is taken as zero when this ratio is zero, it is seen that the phase increases to $+180$ degrees as the ratio increases to plus infinity and decreases to -180 degrees as the ratio goes to minus infinity. If a greater phase shift is required, two or more of the phase shifters may be operated in tandem. The total phase shift of the combination will be the sum of the phase shifts of the individual networks, since the networks have a constant resistance image impedance at each end.

As an illustrative example appropriate values for the elements of the phase shifter shown in Fig. 18 will now be worked out. It will be assumed that the image impedance R_0 is 100 ohms and that a phase shift range of ± 90 degrees is required. If dissipation in the elements is neglected, it is necessary that the reactance X_1 be adjustable from -100 ohms to $+100$ ohms. For example, the adjustable inductance L_1 as shown in Fig. 21 may have a range of 900 ohms to 1100 ohms at the operating frequency f_0 and the capacitance C_1 in series therewith will then have a fixed reactance value of 1000 ohms at that frequency. The combination will thus vary from -100 ohms to $+100$ ohms as the inductance L_1 is adjusted. Now if the effective resistance R_1 is 10 ohms, R_0 is found from Equation 15 to be equal to 101 ohms. From Equation 10 the proper value of the compensating resistance R_2 is found to be 1010 ohms, in order to make the loss of the network independent of the phase setting. The flat loss α is found from Equation 12 to be 1.73 decibels. Now, when dissipation is taken into account, since R_0 is 101 ohms the reactance change will have to be increased from ± 100 ohms to ± 101 ohms to provide the full ± 90 -degree phase shift. In this example the elements of Fig. 18, therefore have the following values:

$$L = \frac{100}{\omega_0} \text{ henries} \quad (16)$$

$$C = \frac{1}{100\omega_0} \text{ farads} \quad (17)$$

$$\frac{L_1}{2} = \frac{1000}{2\omega_0} = \frac{500}{\omega_0} \text{ henries} \quad (18)$$

$$2C_1 = \frac{2}{1000\omega_0} = \frac{1}{500\omega_0} \text{ farads} \quad (19)$$

$$\frac{R_1}{2} = \frac{10}{2} = 5 \text{ ohms} \quad (20)$$

$$\frac{R_2}{2} = \frac{1010}{2} = 505 \text{ ohms} \quad (21)$$

$$\text{where } \omega_0 = 2\pi f_0 \quad (22)$$

and f_0 is the operating frequency.

The phase shifter may, of course, be built in any of the other equivalent forms shown in Figs. 17, 19 and 20 and the elements evaluated by applying the simple factors indicated. The choice of structure may be influenced, among other things, by the behavior of the network at frequencies other than the operating frequency f_0 . The networks shown in Figs. 18 and 20 will pass frequencies below f_0 and tend to suppress frequencies above f_0 , while the reverse is true of the networks of Figs. 17 and 19.

What is claimed is:

1. A variable phase shifter of the bridged-T type comprising two series reactances each of

value X at the operating frequency f_0 , an interposed shunt branch comprising a reactance of value $-X$ at f_0 in parallel with an arm comprising a third reactance of value X in series with the parallel combination of a reactance of value $-2X$ and an adjustable reactive impedance of value Z , and a bridging branch comprising a second reactance of value $-2X$ in parallel with a second adjustable reactive impedance of value Z , X being approximately equal in magnitude to the image impedance R_0 of the phase shifter.

2. A phase shifter in accordance with claim 1 in which X is inductive.

3. A phase shifter in accordance with claim 1 in which X is capacitive.

4. A phase shifter in accordance with claim 1 which includes two resistances each of value $2R_2$ connected in parallel, respectively, with each of said adjustable reactive impedances, R_2 approximately satisfying the relation

$$\frac{1}{R_1} + \frac{1}{R_2} = \frac{R_2}{R_0^2}$$

where R_1 is the effective resistance of each of said adjustable reactive impedances at said frequency f_0 .

5. A phase shifter in accordance with claim 1 in which each of said adjustable reactive impedances comprises the series combination of an inductor and a capacitor.

6. A phase shifter in accordance with claim 5 in which said inductor and said capacitor are resonant at approximately the frequency f_0 when the phase shifter is set for the mean phase shift of the range.

7. A phase shifter in accordance with claim 1 in which each of said adjustable reactive impedances comprises a variable capacitor.

8. A phase shifter in accordance with claim 7 in which said variable capacitors are under unitary control.

9. A phase shifter in accordance with claim 1 in which each of said adjustable reactive impedances comprises a variable inductor.

10. A phase shifter in accordance with claim 9 in which said variable inductors are under unitary control.

11. A phase shifter in accordance with claim 1 in which said adjustable reactive impedances are substantially duplicates of each other.

12. A variable phase shifter of the bridged-T type comprising two series capacitors each of value C , an interposed shunt branch comprising an inductor of value L in parallel with an arm comprising a third capacitor of value C in series with the parallel combination of an inductor of value $2L$ and an adjustable reactive impedance of value Z , and a bridging branch comprising a second inductor of value $2L$ in parallel with a second adjustable reactive impedance of value Z , C and L each having at the operating frequency f_0 a reactance which is approximately equal in magnitude to the image impedance R_0 of the phase shifter.

13. A phase shifter in accordance with claim 12 in which said adjustable reactive impedances are substantially duplicates of each other.

14. A phase shifter in accordance with claim 12 which includes two resistances each of value $2R_2$ connected in parallel, respectively, with each of said adjustable reactive impedances, R_2 approximately satisfying the relation

$$\frac{1}{R_1} + \frac{1}{R_2} = \frac{R_2}{R_0^2}$$

where R_1 is the effective resistance of each of said adjustable reactive impedances at said frequency f_0 .

15. A phase shifter in accordance with claim 12 in which each of said adjustable reactive impedances comprises the series combination of an inductor and a capacitor.

16. A phase shifter in accordance with claim 15 in which said last-mentioned inductor and capacitor are resonant at approximately the frequency f_0 when the phase shifter is set for the mean phase shift of the range.

17. A phase shifter in accordance with claim 12 in which said adjustable reactive impedances are under unitary control.

18. A variable phase shifter of the bridged-T type comprising two series inductors each of value L , an interposed shunt branch comprising a capacitor of value C in parallel with an arm comprising a third inductor of value L in series with the parallel combination of a capacitor of value $C/2$ and an adjustable reactive impedance of value Z , and a bridging branch comprising a second capacitor of value $C/2$ in parallel with a second adjustable reactive impedance of value Z , C and L each having at the operating frequency f_0 a reactance which is approximately equal in magnitude to the image impedance R_0 of the phase shifter.

19. A phase shifter in accordance with claim 18 in which said adjustable reactive impedances are substantially duplicates of each other.

20. A phase shifter in accordance with claim 18 which includes two resistances each of value $2R_2$ connected in parallel, respectively, with each of said adjustable reactive impedances, R_2 approximately satisfying the relation

$$\frac{1}{R_1} + \frac{1}{R_2} = \frac{R_2}{R_0^2}$$

where R_1 is the effective resistance of each of said adjustable reactive impedances at said frequency f_0 .

21. A phase shifter in accordance with claim 18 in which each of said adjustable reactive impedances comprises the series combination of an inductor and capacitor.

22. A phase shifter in accordance with claim 21 in which said last-mentioned inductor and capacitor are resonant at approximately the frequency f_0 when the phase shifter is set for the mean phase shift of the range.

23. A phase shifter in accordance with claim 18 in which said adjustable reactive impedances are under unitary control.

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No references cited.